

J . J . Colle ge of Ar ts and Sc ie nc e (Aut onom ous)

J.J.Nagar, Sivapuram Post, Pudukkottai - 622 422

NAAC Accredited with „A“ Gr

PG - Programme - M.Sc. MATHEMATICS - Under Choice Based Credit System

For the candidates admitted from the academic year 2019-2020 onwards

Sem	Course Code	Course Title	Hours/ Week	Credit	Exam Hours	MARKS
I	P1R1MTCC1	Algebra –I	6	5	3	100
	P1R1MTCC2	Real Analysis –I				
	P1R1MTCC3	Ordinary Differential Equations	6	5	3	100
	P1R1MTCC4	Classical Mechanics	6	5	3	100
	P1R1MTEC1	Elective Course-I (Any one from the choice given below)	6	3	3	100
		TOTAL	30	23		500
II	P2R1MTCC5	Algebra –II	6	5	3	100
	P2R1MTCC6	Real Analysis –II	6	5	3	100
	P2R1MTCC7	Partial Differential Equations	6	5	3	100
	P2R1MTCC8	Topology	6	5	3	100
	P2R1MTEC2	Elective Course-II (Any one from the choice given below)	6	3	3	100
		TOTAL	30	23		500
III	P3R1MTCC9	Fluid Dynamics	6	5	3	100
	P3R1MTCC10	Functional Analysis	6	5	3	100
	P3R1MTCC11	Complex analysis	6	5	3	100
	P3R1MTCC12	Measure Theory and Integration	6	5	3	100
	P3R1MTEC3	Elective Course-III (Any one from the choice given below)	6	3	3	100
		TOTAL	30	23		500
IV	P4R1MTCC13	Stochastic Processes	6	5	3	100
	P4R1MTCC14	Optimization Techniques	6	5	3	100
	P4R1MTCC15PW	Project	12	8	*	100
	P4R1MTEC4P	Elective Course-IV (Any one from the choice given below)	6	3	3	100
		TOTAL	30	21		400
		GRAND TOTAL		90		1900

ELECTIVE PAPERS:

Any **Four** to be chosen as EC1, EC2, EC3 and EC4

I Semester

- Calculus of Variation and Integral Equations
- Advanced Number Theory
- Fuzzy Mathematics and its Applications

II Semester

- Numerical Analysis
- Automata Theory
- Combinatorial Mathematics

III Semester

- Applied Mathematical Statistics
- Integrals of Special Functions
- Advanced Graph Theory

IV Semester

- Advanced MATLAB
- Graph Algorithm

SEM –I
Hours/Week: 6
Credit : 5
Total Hours: 72

M.Sc. MATHEMATICS
ALGEBRA- I
CODE:P1R1MTCC1

CORE COURSE:1
Int. Marks: 25
Ext. Marks: 75
Max. Marks: 100

Objectives:

- To educate the advanced level of Groups
- To understand the sequential development of Abelian group concepts and skills by using materials for making the transition from the arithmetic to the symbolic.
- To understand the concepts of Ring, Euclidean Ring.
- To have a brief study of polynomial Rings
- To study the algebraic structure of finite fields.

Unit I: Group Theory (16 Hours)

Introduction to Group Theory: Basic Definitions in Groups – Permutation Groups – Problems in Permutation Groups – Another counting Principle – Conjugate – Normalizer – Applications – Sylow's theorem .

Unit II: Abelian Group (14 Hours)

Direct Product: Internal Direct Product and External direct Product – Normal Group – Center of Groups – Introduction to Abelian Groups: Finite abelian groups – Invariants – Partition – Orders - Properties of Isomorphism in Abelian Groups.

Unit III: Ring Theory (14 Hours)

Introduction: Ring and Field – Integral Domain – The field of Quotients of an Integral domain – Euclidean Rings – Greatest common divisor – Unit – Associates – A Particular Euclidean Rings – Fermat's Theorem.

Unit IV: Polynomial Rings (14 Hours)

Definition for Ring of Polynomials – Properties of Polynomial Rings – Degree – irreducible – Polynomials over the Rational Field: Primitive Polynomials – Content – Integer Monic – Polynomial Rings over commutative rings: Unique Factorization domain.

Unit V: Finite Field (12 Hours)

Finite fields – Wedderburn's theorem – On a theorem of Frobenius .

Unit –VI: (02 Hours)

Latest development related to the course during the semester concerned. [For purpose of Continuous Internal Assessment only]

Text Book :

[1] I.N.Herstein, „Topics in Algebra“, Second

Unit I - Chapter 2 (Section 2.10 –2.12)

Unit II - Chapter 2 (Section 2.13 –2.14)

Unit III- Chapter 3 (Section 3.6 –3.8)

Unit IV- Chapter 3 (Section 3.9 –3.11)

Unit V - Chapter 7 (Section 7.1 –7.3)

Reference Books:

1. Surjeet Singh, Quazizameeudui, „Modern Algebra“, Vikas Publ
2. J. Gallian, „Contemporary Abstract Algebr

Outcomes:

The learners would have the ability to

- Acquire knowledge on the metric spaces.
- Apply the mean value theorems in a correct mathematical way.
- Study Cauchy sequence, upper and lower limits of number sequence.
- Learn series , power series, absolute convergence and rearrangements.
- Understand continuity, compactness and monotonic functions.

SEM –I
Hours/Week: 6
Credit : 5
Total Hours: 72

M.Sc. MATHEMATICS
REAL ANALYSIS- I
CODE:P1R1MTCC2

CORE COURSE:2
Int. Marks: 25
Ext. Marks: 75
Max. Marks: 100

Objectives:

- To deal primarily with sequences and series of complex numbers.
- To discuss vector valued functions (i.e. functions with values in $\mathbb{R}^k$) and functions with values in an arbitrary metric space.
- To confine our attention to real functions defined on intervals or segments.
- To understand numerical series and power series.
- To focus on continuity and connectedness.

Unit I: Metric Spaces

(14 Hours)

Examples of Metric Spaces - Open sets, Closed sets and Convergent sequences - Continuous mappings between metric spaces - Complete metric spaces –Compact metric spaces.

Unit II: Basic Topology

(14 Hours)

Finite, Countable and Uncountable Sets –Metric Spaces –Compact Sets, Weirstrass Theorem –Perfect Sets, The Cantor Set –Connected Sets.

Unit III: Numerical Sequences

(12 Hours)

Convergent Sequences –Subsequences –Cauchy Sequences –Upper and Lower Limits –Some Special Sequences.

Unit IV: Numerical Series

(16 Hours)

Series –Series of Nonnegative Terms - The Number e –The Root and Ratio Tests – Power Series –Summation by Parts –Absolute Convergence –Addition and Multiplication of Series –Rearrangements.

Unit V: Continuity

(14 Hours)

Limits of Functions – Continuous Functions – Continuity and Compactness – Continuity and Connectedness –Discontinuities –Monotonic functions –Infinite Limits and Limits at Infinity.

Unit –VI:

(02 Hours)

Latest development related to the course during the semester concerned. [For purpose of Continuous Internal Assessment only]

Text Books:

[1] “Principles of Analysis”, Walter Rudin-McGraw Hill Education, 3rd Edition, 2013.

[2] “ Real Analysis”, H.L. Royden, P.M. Fitz

Unit I : Chapter 9 –9.1 to 9.5 [2]

Unit II: Chapter 2 [1]

Unit III: Chapter 3(Page No. 47 - 58)[1]

Unit IV: Chapter 3(Page No. 58 - 77) [1]

Unit V: Chapter 4 [1]

Reference Books:

[1] T.M. Apostol, Mathematical Analysis, Narosa Publ. House, New Delhi, 1985.

[2] H.L. Royden, Real Analysis, Macmillan Publ. Co. Inc. 4th edition, New York, 1993.

[3] V. Ganapathy Iyer, Mathematical Analysis, Tata McGraw Hill, New Delhi, 1970.

Outcomes:

The learners would have the ability to

- Acquire knowledge on the metric spaces.
- Apply the Mean value theorems in a correct Mathematical way.
- Study cauchy's sequence ,upper sequences. and lower lim
- Learn series, power series Absolute convergent and rearrangement.
- Understand continuity compactness and monotonic functions.

SEM –I	M.Sc. MATHEMATICS	CORE COURSE:3
Hours/Week: 6	ORDINARY DIFFERENTIAL EQUATIONS	Int. Marks: 25
Credit : 5	CODE:P1R1MTCC3	Ext. Marks: 75
Total Hours: 72		Max. Marks: 100

Objectives

- To identify an ordinary differential equation and its order.
- To find solutions of separable differential equations.
- To find the general solution of second order linear homogeneous equations with constant coefficients .
- To find solution of DE using Laplace Transforms.
- To use successive approximations.

Unit I: Second Order Linear Equations (16 Hours)

Introduction - The General Solution of Homogeneous Equation - The use of a Known Solution to find another - Homogeneous equation with constant coefficients –The Method of Undetermined Co-efficients - The method of Variation of parameters.

Unit II: Power Series Solutions and Special Functions (14 Hours)

Introduction-Series solutions of First order equations-Second order Linear equations - Ordinary points - Regular singular points - Regular singular points (continued).

Unit III: Some Special Functions (12 Hours)

Legendre Polynomials - Properties of Legendre polynomials - Bessel Function, The Gamma Function - Properties of Bessel Functions.

Unit IV: Laplace Transforms (14 Hours)

Introduction- A few remarks on the theory –Applications to Differential Equations - Derivatives and Integrals of Laplace Transforms –Convolutions and Abels Mechanical Problem.

Unit V:The Existence And Uniqueness Of Solutions (14 Hours)

The method of successive Approximations –Picard’s Theorem –the second order linear Equations.

Unit –VI: (02 Hours)

Latest development related to the course during the semester concerned. [For purpose of Continuous Internal Assessment only]

Text Book:

[1] **Differential “ Equations with Applications and Historical notes”** Georgeby Simmons, Tata Mc GrawHill, Second Edition 2003, 22nd Reprint 2012.

Unit I:Chapter 3 - Sec 14 to 19

Unit II :Chapter 5-Sec 26 to 30

Unit III:Chapter 8-Sec 44 to 47

Unit IV:Chapter 9 - Sec 48 to 52

Unit V :Chapter 13 - Sec 68 to 70

Reference Books:

[1] W.T. Reid, “Ordinary”, John Differential Wiley&Sons, New York, 1971. Equations

[2] E.A. Coddington and N. Levinson, “McGraw” Theory Hill of Publishing Company, New York, 1955.

Outcomes :

The learners would have the ability to

- Use the method of variation of parameters to find particular solutions of second order, linear homogeneous equations.
- Use the method of undetermined co-efficient to solve 2nd order linear homogeneous equations.
- Learn about Legendre Polynomials, Bessels function and Gamma functions
- Acquire the knowledge of apply the Laplace transform to solve the simultaneous linear equations.
- Use the method of successive approximation Picards theorem.

SEM –I
Hours/Week: 6
Credit : 5
Total Hours: 72

M.Sc. MATHEMATICS
CLASSICAL MECHANICS
CODE:P1R1MTCC4

CORE COURSE:4
Int. Marks: 25
Ext. Marks: 75
Max. Marks: 100

Objectives

- To understand and deals with some of the key ideas of classical mechanics.
- To understand the concepts covered in the course include generalized coordinates, Lagrange's equations, Hamilton's-Jacobi theory. equation
- To develop skills in formulating and solving physics problems.
- To represent the equations of motion for complicated mechanical systems using the Lagrangian.
- To study Hamiltonian formulations of classical mechanics.

Unit I: ELEMENTARY PRINCIPLES

(14 Hours)

Mechanics of a Particle - Mechanics of a system of particles –Constraints – D'Alembert's principle and principle of Lagrange's –Velocity-Dependent equation potentials and the dissipation function –Simple Application of the Lagrangian formulation.

Unit II: CENTRAL FORCE PROBLEM

(16 Hours)

Reduction to the equivalent one - Body problem –The equation of motion and first integrals –The equivalent one - Dimensional problem and Classification of Orbits –The Virial theorem – The Differential equation for the Orbit and Integrable power- Law Potentials.

Unit III: The Kepler Problem

(12 Hours)

Inverse square law of force –The motion in time in the Kepler Problem –The Laplace-Runge-Lenz vector –Scattering in a Central Force Field.

Unit IV: The Kinematics of Rigid Body Motion

(14 Hours)

The independent coordinates of a rigid body –Orthogonal Transformation –Formal Properties of the transformation Matrix –The Euler Angles –The Cayley –Klein parameters and related quantities –Euler's theorem on the motion of a rigid body.

Unit V: The Hamilton Equation of Motion

(15 Hours)

Legendre Transformation and the Hamilton equations of motion –Cyclic Coordinates and conservation Theorems –Routh Procedure – The Hamiltonian Formulation of Relativistic Mechanics –Derivation of Hamilton's Variational Principle Equation.

Unit –VI:

(01 Hours)

Latest development related to the course during the semester concerned. [For purpose of Continuous Internal Assessment only]

Text Book:

[1] Classical Mechanics, by Herbert Goldstein and others
Edition 2013, New Delhi.

Unit I: Chapter 1 –Sec 1.1 to 1.6

Unit II: Chapter 3 –Sec 3.1 to 3.5

Unit III: Chapter 3 –Sec 3.7 to 3.10

Unit IV: Chapter 4 –Sec 4.1 to 4.6

Unit V: Chapter 8 –Sec 8.1 to 8.5

Reference Books:

[1] Classical Dynamics by Donald T. Greenwood, PHI Pvt. Ltd., New Delhi-1985.

[2] Classical Mechanics by Narayanan Chandra Rana and Hill. 1990.

Outcomes:

The learners would have the ability to

- Have a deep understanding of Mechanics of a system of particles and D'Alembert's principle.
- Be able to solve the DE for the orbit.
- Be familiar with Kepler problem used in physics.
- Know about Euler's Equation on the notation
- Study about Routh procedure to derive Hamilton's Equations..

SEM –II
Hours/Week: 6
Credit : 5
Total Hours: 72
Objectives:

M.Sc. MATHEMATICS
ALGEBRA –II
CODE: P2R1MTCC5

CORE COURSE:5
Int. Marks: 25
Ext. Marks: 75
Max. Marks: 100

- To develop mathematical maturity and ability on fields.
- To study algebraic structure of a linear transformation.
- To study Canonical forms.
- To educate advanced level of finite fields.
- To be better equipped in Canonical forms of various transformations.

UNIT I: Vector Spaces (14 Hours)

Linear Functional and the Dual space - Linear functional and its examples - Dual basis, Reflexivity, Annihilator, Transpose of a linear map - Reflexivity Theorem and solved examples

UNIT II: Extension Fields (16 Hours)

Extension - Finite extension –Algebraic extension - splitting field, Algebraic closure –Root field –Root of a polynomial of multiplicity m - Degree of an algebraic number – Derivative of a polynomial, Separable. (Theorems & Problems)

UNIT III: Galois Theory (14 Hours)

Automorphism of a field –Normal extension, Fixed field –Elementary symmetric functions –Galois group for a polynomial –Conjugate elements (Theorems and Problems).

UNIT IV: Modules (12 Hours)

Definition –Types of modules –algebra of modules –Direct sum of sub modules (Theorems & Problems)

UNIT V: Canonical Forms and Nil Potent Operators (14 Hours)

Similarity of matrices and linear maps invariant subspaces –Normal form, Triangular form–Invariant direct sum decomposition –Nil potent transformations.

Unit –VI: (02 Hours)

Latest development related to the course during the semester concerned. [For purpose of Continuous Internal Assessment only]

TEXT BOOK:

[1] “Advanced Course in Modern Algebra”, 8th edition 2015. Goyal

Unit I : Chapter 12 – Part 5 (Page No. 546-565)

Unit II : Chapter 13 –(Sec 1,2,3 & 4 Only) (Page No. 566- 596)

Unit III : Chapter 14 –(Sec 1 -3) (Page No. 609- 631)

Unit IV :Chapter 16 –(All Sections) (Page No. 656- 680)

Unit V : Chapter 19 –(All Sections) (Page No. 703- 727)

Reference Books:

[1] „Abstract Algebra“, David S.Dummit and edition, 2004.

[2] „Algebra“, HirdSergeEdition, SpringerLang,–2002.Revised T

Outcomes :

The learners would have the ability to

- Have a deep understanding of vector spaces.
- Understand the concept of Extension field, Splitting field and Root field.
- Explain the notion of Galois Theory.
- Describe the structure of modules.
- Apply the concept of the Decomposition and Nilpotent transformations.

SEM –II
Hrs/Week: 6
Credit : 5
Total Hrs: 72
Objectives:

M.Sc. MATHEMATICS
REAL ANALYSIS - II
Code: P2R1MTCC6

CORECOURSE:6
Int.Marks: 25
Ext.Marks: 75
Max.Marks:100

- To be familiar with the advanced concepts of Real Analysis.
- To give a systematic study of Riemann stieltjes integral and calculus on R^n .
- To have a brief study of convergence of sequences and series, Functions of several variables.
- To study Fourier Series and Gamma Function.
- To apply the contraction principle.

Unit I: Differentiation

(15 Hours)

The derivative of a Real function –Mean value theorems –The Continuity of the derivatives – L’ Hospital’s–Derivatives of higher order –Taylor’s– theorem
Differentiation of vectors valued functions.

Unit II: Reimann- Stieltjes integral

(13Hours)

Definition and existence of the Integral –Properties of the Integral –Integration and Differentiation- Integration of vector –valued Functions.

Unit III: Sequences and Series of functions

(14 Hours)

Discussion of main problem –Uniform convergence – Uniform convergence and Continuity – Uniform convergence and Integration – Uniform convergence and Differentiation - Equi-continuous families of functions –The Stone-Wierstrass theorem.

Unit IV: Some Special Functions

(14 Hours)

Power series –The Exponential and Logarithmic Functions –The Trigonometric Functions –The Algebraic Completeness of the Complex Field –Fourier Series –The Gamma Function.

Unit V: Functions of Several variables

(12 Hours)

Linear Transformations –Differentiations –The contraction Principle- The inverse function theorem –The Implicit Function Theorem.

Unit –VI:

(02 Hours)

Latest development related to the course during the semester concerned. [For purpose of Continuous Internal Assessment only]

Text Books:

[1] “ Principles of Mathematical Analysis”,

Unit I : Chapter 5- Sec 5.1 to 5.19

Unit II: Chapter 6- Sec 6.1 to 6.25

Unit III: Chapter 7 - Sec 7.1 to 7.27

Unit IV: Chapter 8 - Sec 8.1 to 8.22

Unit V: Chapter 9 - Sec 9.1 to 9.29

Reference Books:

[1] “Mathematical Analysis”, Tom P. Apostol,

[2] “AnalysisLang,IAAddisonand–WesleyII”,PublishingSergeCompany, 1969.

Outcomes:

The learners would have the ability to

- Study in detail the Mean .value theorem a
- Acquire knowledge on Differentiations and Integrations.
- Learn Cauchy’s superior sequences, and Limit inferior. Limit
- Understand the concepts of power series –Fourier series.
- Study inverse function theorem and implicit function theorem.

SEM –II
Hrs/Week: 6
Credit : 5
Total Hrs: 72

M.Sc. MATHEMATICS
Partial Differential Equations
Code: P2R1MTCC7

CORECOURSE:7
Int.Marks: 25
Ext.Marks: 75
Max.Marks:100

Objectives:

- To classify Partial differential equations into linear and nonlinear equation.
- To understand the notion of linear independence and the notion of a fundamental set of solutions.
- To use the Laplace transform to compute solutions of equations involving impulse functions.
- To find solutions of the heat equation, wave equation, and the Laplace equation subject to boundary conditions.

Unit I: First Order PDE

(14 Hours)

First order PDE - Curves and surface - Genesis of first order PDE - Classification of Integrals - Linear equation of the first order - Pfaffian Differential equations - Compatible systems - Charpits method –Jacobi's method.

Unit II: cntd. of First Order PDE

(12 Hours)

Integral surfaces through a given curve - Quasi - Linear equations - Non linear First order PDE.

Unit III: Second Order PDE

(14 Hours)

Genesis of second order PDE - Classification of Second order PDE: One - Dimensional wave equation - Vibrations of an Infinite string - Vibrations of semi - infinite string – Vibrations of a string of finite length(Method of separation of variables).

Unit IV: Laplace's Equation

(16 Hours)

Boundary value problems - Maximum and Minimum Principles - The Cauchy problem - The Dirichlet problem for the upper half plane - The Neumann problem for the upper half plane - The Dirichlet problem for a circle - The Dirichlet exterior problem for a circle - The Neumann problem for a circle - The Dirichlet problem for a Rectangle - Harnack's theorem - Laplace's Green's function.

Unit V: Heat Conduction

(14 Hours)

Heat Conduction problem –Heat conduction - Infinite Rod case - Heat conduction finite rod case - Duhamel's - Wave principle equation - Heat conduction equation.

Unit –VI:

(02 Hours)

Latest development related to the course during the semester concerned. [For purpose of Continuous Internal Assessment only]

TEXT BOOK:

[1] "An Elementary Course in Partial Differential equations" by T. Amarnath, Narosa, 1997.

Unit I: Chapter 1-Sec 1.1 to 1.8

Unit II : Chapter 1-Sec 1.9 to 1.11

Unit III : Chapter 2- Sec 2.1 to 2.3.5(except 2.3.4)

Unit IV : Chapter 2- Sec 2.4.1 to 2.4.11

Unit V: Chapter 2-Sec 2.5.1, 2.5.2, 2.6.1 and 2.6.2

Reference Books:

[1] "Elements of Partial Differential Equations", [2] "Partial Differential Equations", P. Prasad

Outcomes:

The learners would have the ability to

- Able to solve first order linear differential equation by Method
- Understand the quasi linear equations and non linear first order PDE.
- Acquire knowledge to solve second order PDE.
- Understand the Laplace transform to compute solutions of equations involving impulse functions.
- Learn about Duhamel's heat conduction principle equation, and wave and

SEM –II
Hours/Week: 6
Credit : 5
Total Hours: 72
Objectives:

M.Sc. MATHEMATICS
TOPOLOGY
CODE:P2R1MTCC8

CORE COURSE:8
Int. Marks: 25
Ext. Marks: 75
Max. Marks: 100

- To develop and understand Topological spaces including connectedness and compactness.
- To study the continuous functions on the topological spaces and study their homeomorphisms.
- To study regular second countable spaces which are metrizable.
- To be familiar with compactness.
- To understand countability axioms and normal spaces.

Unit I: Topological Spaces (14 Hours)

Topological Spaces –Basis for a Topology –The Order Topology –The Product Topology on $X \times Y$ –The Subspace topology –Closed sets and Limit points.

Unit II: Continuous Functions (13 Hours)

Continuous functions –The Product topology –The metric Topology –The metric Topology (continued).

Unit III: Connectedness (14 Hours)

Connected Spaces –Connected subspaces of the Real line, Linear Continuum, Intermediate Theorem –Components and Local connectedness.

Unit IV: Compactness (15 Hours)

Compact spaces –The Tube Lemma –Compact Subspaces of the Real line – Extreme Value Theorem, Uniform Continuity Theorem –Limit Point Compactness- Local compactness.

Unit V: Countability and Separation Axioms (14 Hours)

The Countability axioms – The Separation axioms – Normal Spaces – The Uryshon lemma- The Uryshon Metrization theorem- The Tietz Extension theorem.

Unit –VI: (02 Hours)

Latest development related to the course during the semester concerned. [For purpose of Continuous Internal Assessment only]

Text Book:

[1]Topology”, “ James R. Munkres, (2002)Pearson Educa
Unit I: Chapter 2, Sec 12 to 17
Unit II: Chapter 2, Sec 18 to 21
Unit III: Chapter 3, Sec 23 to 25
Unit IV: Chapter 3, Sec 26 to 29
Unit V: Chapter 4, Sec 30 to 35.

Reference Books:

- [1] “Topology”, J. Dugunji, Prentice Hall of
- [2] “Introduction to Topology and Modern Analy Book co.,1963.
- [3] “General Topology” J. C. Kelly, Van Nost

Outcomes:

The learners would have the ability to

- Obtain the knowledge of fundamental concepts and methods in general topology.
- Acquire knowledge about product topology and metric topology .
- Know about connectedness and intermediate theorem.
- Study about compactness-extreme value theorem and uniform continuity theorem.
- Learn about normal spaces and Tietz extension theorem.

SEM –III
Hours/Week: 6
Credit : 5
Total Hours: 72

M.Sc. MATHEMATICS
FLUID DYNAMICS
CODE:P3R1MTCC9

CORE COURSE:9
Int. Marks: 25
Ext. Marks: 75
Max. Marks: 100

Objectives:

- To introduce the fundamentals of fluid Dynamics such as kinematics of fluid, incompressible flow and boundary layer flows
- To discuss of the case of steady motion under conservative body forces and Some Potential Theorems
- To develop skills in formulating and solving physics problems.
- To study two- dimensional flows.
- To introduce viscosity and show what are Newtonian and non-Newtonian fluids

Unit I: Kinematics of Fluids in Motion (13 Hours)

Real fluids and Ideal Fluids –Velocity of a fluid at a point –Streamlines and Path lines;
Steady and Unsteady flows - Velocity Potential –Vorticity Vector –Local and Particle rates of change
–The Equations of Continuity –Worked Examples.

Unit II: Equations of Motions of a Fluid (15 Hours)

Pressure at a point in a fluid at rest –Pressure at a point in a moving fluid –Conditions at a boundary at Two in viscid immiscible fluids –Euler’s Equation–Bernoulli’s–Motion Equ
Worked Examples –Discussion of the case of steady motion under conservative body forces –Some Potential Theorems –Some flows involving Axial Symmetry.

Unit III: Some Three Dimensional Flows (14 Hours)

Introduction –Source, Sinks and Doublets, Images in a rigid infinite plane –Images in Solid spheres –Axi-Symmetric Flows: Stoke’s–Some special forms stream of the function for Axi-Symmetric irrotational motion.

Unit IV: Some Two Dimensional Flows (15 Hours)

Complex Velocity Potentials For Standard Two –Dimensional Flows –Uniform Stream – Line Sources and Line Sinks –Line Doublets –Line Vortices –Some Worked Examples –Two Dimensional Image System –Milne-Thomson Circle Theorem –Theorem of Blasius.

Unit V: Viscous Flow (13 Hours)

Viscous flow –Some solvable problems in viscous flow –Steady viscous flow in Tubes – Steady viscous flow in Tubes of Uniform cross-section.

Unit –VI: (02 Hours)

Latest development related to the course during the semester concerned. [For purpose of Continuous Internal Assessment only]

Text Book:

[1] “Text Book of fluid Dynamics”, by Charlton,

Unit I :Chapter 2 Sec 2.1 to 2.8

Unit II :Chapter 3 Sec 3.1 to 3.9

Unit III : Chapter 4 Sec 4.1 to 4.5

Unit IV :Chapter 5 Sec 5.5 to 5.9

Unit V :Chapter 8 Sec 8.10 and 8.11

Reference Books:

[1] “Introduction to Fluid Mechanics”, R.W.Fox a

[2] “Fluid Mechanics with Problems and Solutions

[3] “Mechanics of Fluids”, B.S.Massey, J.W.Smith

Outcomes:

The learners would have the ability to

- Recognize the principles written in form of mathematical equations in fluid dynamics.
 - Apply dimensional analysis to predict physical parameters that influence the flow in fluid mechanics using potential theorems.
 - Understand Stoke’s stream function.
 - Study Milne-Thomson circle theorem and theorem of Blasius.
- Acquire knowledge of steady of viscous flows.

SEM –III
Hours/Week: 6
Credit : 5
Total Hours: 72
Objectives:

M.Sc. MATHEMATICS
FUNCTIONAL ANALYSIS
Code:P3R1MTCC10

CORE COURSE:10
Int. Marks: 25
Ext. Marks: 75
Max. Marks: 100

- To understand the definition and fundamental properties of metric spaces, including the ideas of convergence, continuity, completeness, compactness and connectedness
- To understand the definition and fundamental properties of Hilbert spaces, and bounded linear maps between them
- To generalize the basic concepts of geometry and linear algebra can be generalized to infinite dimensional spaces
- To study Banach Algebras.
- To study picard's theorem and stone's theor

Unit I : Banach Spaces (16 Hours)

The definition and some examples –continuation linear transformations –The Hahn-Banach theorem –The natural imbedding of N in N^{**} –The open mapping theorem –The conjugate of an operator.

Unit II: Hilbert Spaces (15 Hours)

The definition and some simples properties –orthogonal complements –orthonormal sets –the conjugate space H^* – The adjoint of an operator –self-adjoint operators – normal and unitary operators –projections.

Unit III: Finite Dimensional Spectral Theory (12 Hours)

Matrices –Determinants and the spectrum of an operator –The spectral Theorem –A survey of the situation.

Unit IV:General Preliminaries on Banach Algebras (13 Hours)

The definition and some examples –Regular and singular elements –Topological divisors of zero –the spectrum –the formula for the spectral radius – the radical and semi – simplicity.

Unit V: The Fixed Point Theorems and Boolean Algebras(Appendices) (14 Hours)

Fixed point theorem –Brouwer's fixed point theorem, schauder's fixed– p
 Picard's –Booleanththeorem algebra –Boolean rings –stone's theorem.

Unit –VI: (02 Hours)

Latest development related to the course during the semester concerned. [For purpose of Continuous Internal Assessment only]

Text Book:

[1] “Introduction to topology and Modern Analys (India) Edition 2004.

Unit I : Chapter 9 Fully (page No. 211-242)

Unit II : Chapter 10 Fully (Page No. 243-277)

Unit III : Chapter 11 Fully (Page No. 278-297)

Unit IV : Chapter 12 Fully (Page No. 301-317)

Unit V : Appendices 1 and 3 (Page No. 337-340 & 344-353)

Reference Books:

[1] “Functional Analysis ”,Walter Rudin, TMH Ed

[2] “Functional Analysis”,Functional Analysis,WileyBEastern.V limited,Linaye,Bombay,second Edition 1985

Outcomes: The learners would have the ability to

- Understand the concept of Banach spaces & Hilbert spaces.
- Acquire knowledge about Hilbert spaces.
- Describe the structure of finite dimensional spectral theory.
- Study about Regular, singular elements and the spectrum.
- Learn about fixed point theorem, picard's the

SEM –III
Hours/Week: 6
Credit : 5
Total Hours: 72

M.Sc. MATHEMATICS
COMPLEX ANALYSIS
Code:P3R1MTCC11

CORE COURSE:11
Int. Marks: 25
Ext. Marks: 75
Max. Marks: 100

Objectives:

- To understand the concepts of Analytical function.
- Apply Cauchy's integral formula to evaluate
- Expand functions in theorems of Taylor's and Weierstrass
- Apply the Residue theorem to evaluate real integrals.
- To use the two dimension Laplace's-ordinates equation to determine whether a real valued is harmonic or not.

Unit I: Complex functions (14Hours)

Introduction to the concept of Analytical function –Elementary theory of Power series –The exponential and Trigonometric Functions.

Unit II: Fundamental Theorems and Cauchy's Integral (16 Hours) Formula

Line Integrals - Rectifiable –Line Integrals Arc's as Functions of Arcs - Cauchy's Theorem for a Rectangle –Cauchy's Theorem Disk –Index in of a point with respect to a closed curve –The Integral Formula –Higher Derivatives.

Unit III: Local Properties of Analytic Functions (12Hours)

Removable singularities, Taylor's –Zeros and Theorem Poles –Weierstrass Theorem –The Local Mapping –The Maximum Principle –Schwarz Lemma.

Unit IV: General Form of Cauchy's Theorem Residues (14Hours) and t

Chains and Cycles –Simple Connectivity –Locally Exact Differentials –Multiply Connected Regions –The Residue Theorems –The Argument Principle –Evaluation of Definite Integrals.

Unit V: Harmonic Function (14 Hours)

Definition and Basic Properties –Interpretation –The Mean Value Property –Maximum Principle –Poisson's –Schwarz's Formula –The Theorem Reflection Principle.

Unit –VI: (02 Hours)

Latest development related to the course during the semester concerned. [For purpose of Continuous Internal Assessment only]

Text Book:

[1] "Complex Analysis", Lars V. Ahlfors, III e

Unit I : Chapter 2 –All sections

Unit II : Chapter 4- Sec 1(1.1 to 1.5), Sec 2 (2.1 to 2.3)

Unit III : Chapter 4- Sec 3(3.1 to 3.4)

Unit IV : Chapter 4- Sec 4(4.1, 4.2, 4.6 and 4.7) and Sec 5(5.1 to 5.3)

Unit V : Chapter 4- Sec 6(6.1 to 6.5)

Reference Books:

[1] "Complex Analysis", Sarge Lang, Addison W

[2] "Foundations of Complex Analysis", S.P Delhi.

[3] "Complex Analysis", V. Karunakaran,.

Outcomes :

The learners would have the ability to

- Recognize the concept of Analytical function.
- Study Cauchy's theorem for a rectangle in
- Use Taylor's theorem and the maximum prin
- Have a deep understanding of Residues to evaluate definite integrals.
- Know about Schwarz's theorem and reflecti

SEM –III	M.Sc. MATHEMATICS	CORE COURSE:12
Hours/Week: 6	MEASURE THEORY AND INTEGRATION	Int. Marks: 25
Credit : 5	Code:P3R1MTCC12	Ext. Marks: 75
Total Hours: 72		Max. Marks: 100

Objectives:

- To understand the concept of Measure Theory, Definitions and Main Properties of the Integral.
- To construct Lebesgue's Measure–dimension Euclidean on a $\mathbb{R}^n$ Space.
- To overcome the limitation using more abstract space.
- To provide a concise introduction to Measure Theory in the context of Abstract Algebra.
- To Focus on the Development of Measure and Integration Theory.

Unit I : Measure on Real Line (14 Hours)

Lebesgue outer measure –Measurable sets –Regularity –Measurable Functions – Borel and Lebesgue Measurability.

Unit II : Integration of Functions of a Real Variable (14 Hours)

Integration of non-negative functions –The General Integral - Integration of Series – Riemann and Lebesgue Integrals.

Unit III : Convergence (14 Hours)

Measures and Outer Measures –Extension of a Convergence in Measure –Almost Uniform Convergence –Measure –Uniqueness of the Extension.

Unit IV : Signed Measures and their Derivatives (14 Hours)

Hahn Decomposition Theorem –The Jordan Decomposition –The Radon Nikodym Theorem.

Unit V : Measure & Integration in a Product Space (14 Hours)

Measurability in a product space –The Product Measure and Fubini's Theorem.

Unit –VI: (02 Hours)

Latest development related to the course during the semester concerned. [For purpose of Continuous Internal Assessment only]

Text Book:

[1] Measure Theory and Integration –New Age International Private Ltd.

Unit I : Chapter 2, Sec 2.1 –2.5

Unit II : Chapter 3, Sec 3.1 –3.4

Unit III : Chapter 5, Sec 5.1 –5.3 and Chapter 7, Sec 7.1 –7.2

Unit IV : Chapter 8, Sec 8.1 –8.3

Unit V : Chapter 10, Sec 10.1 –10.2

Reference Books:

[1] Introduction to Measure and Integration –Inderjit K. Rana, Narosa Publishing House –New Delhi - 1997.

[2] “Lebesgue Measure–P.K.Jain, V.and P.Gupta –Integration” New Age International Pvt. Ltd – 2000

Outcomes:

The learners would have the ability to

- Understand basis of measure theory
- Study about Riemann and Lebesgue integrals.
- Acquire the knowledge of convergence in measure.
- Understand the Hahn decomposition theorem & Jordan decomposition theorem.
- Learn about measurability and Fubini's theorem

SEM –IV
Hours/Week: 6
Credit : 5
Total Hours: 72
Objectives:

M.Sc. MATHEMATICS
STOCHASTIC PROCESSES
CODE:P4R1MTCC13

CORE COURSE:13
Int. Marks: 25
Ext. Marks: 75
Max. Marks: 100

- To understand the notion of a Markov chain.
- To understand how simple ideas of conditional probability can be used to give a thorough and effective account of discrete-time Markov chains.
- To apply these ideas to answer basic questions in several applied situations including genetics, branching processes and random walks.
- To develop skills in analysing and interpreting the results.
- To discuss steady state Transient behaviour of M/M/1 model.

Unit I: Stochastic Processes

(14 Hours)

Introduction –Specification of Stochastic processes –Stationary Processes –stationary – Gaussian processes - Markov Chains –Definitions and Examples –Higher Transition Probabilities –Generalization of Independent Bernoulli trials –Sequence of Chain –Dependent trails.

Unit II : Classification of states and chains

(14 Hours)

Communication relations –class property –classification of chains –transient and Persistent (recurrent) states –related theorems - Determination of Higher Transition Probabilities –Stability of a Markov system –Stationary distribution –Theorem and problems.

Unit III : Markov Processes with Discrete State space

(14 Hours)

Poisson Process –Postulates for poisson process –Theorems and problems –Properties of poisson process –Poisson processes and related distributions –Generalisation of poisson process – Time dependent poisson processes –Birth and death process.

Unit IV: Renewal Processes and Theory

(12 Hours)

Renewal Process in discrete time –Relation between $F(s)$ and $P(s)$ - Renewal Processes in continuous time –Renewal equation –Stopping time –Wald's –Renewal equation theorems.

Unit V: Stochastic Processes in Queuing

(16 Hours)

Queuing systems: General concepts –Queueing processes –steady state distribution – Little's –The formula Queueing model M/M/1: study state behavior –steady state solution –waiting time distributions –Transient behavior of M/M/1 model.

Unit –VI:

(02 Hours)

Latest development related to the course during the semester concerned. [For purpose of Continuous Internal Assessment only]

Text Book:

[1] J. Medhi, "Stochastic- Wiley Processes", Eastern limited, Chennai. Second ed

Unit I: Chapter 2 –Sec 2.1 to 2.3 (Pg.No.56-63),
Chapter 3–Sec 3.1 and 3.2 (Pg no.69-83)

Unit II : Chapter 3 –Sec 3.4 to 3.6 (Page No.88-112) **Unit**

III : Chapter 4 –Sec 4.1 to 4.4 (Page No.157-192) **Unit IV**

: Chapter 6 - Sec 6.1 to 6.5.1 (Page No.242-264)

Unit V : Chapter 10 - Sec 10.1 to 10.2.2, 10.3.1 (Page No.407-417, 421-424)

Reference Books:

[1] "A First course", Samuelin Kolri Stochastic, Howard M. Taylor, 2 Edition Processes.

[2] "Stochastic", Srinivasan and Processes Medha, N.V Prabhu, Macmillan (NY),

Outcomes: The learners would have the ability to

- Acquire the knowledge of stochastic process, transition probabilities.
- Understand transient and persistent state, stability of a Markov system.
- Be familiar with Poisson process –Birth and death process.
- Know about renewal process and renewal theorem.
- Study about Queuing system –M/M/1: steady state behavior.

SEM –IV
Hours/Week: 6
Credit : 5
Total Hours: 72
Objectives:

M.Sc. MATHEMATICS
OPTIMIZATION TECHNIQUES
Code:P4R1MTCC14

CORE COURSE:14
Int. Marks: 25
Ext. Marks: 75
Max. Marks: 100

- To describe the need and importance of Operations Research.
- To discuss the basic concepts and techniques for solving particular Operations Research problem.
- To develop a research proposal using the general approach for Operations Research.
- To maximize the utility of limited resources.
- To use simulation in investment and budgeting.

UNIT I: Integer Programming (14 Hours)

Introduction –Pure and Mixed Integer programming problems –Gomory’s–I.P. P. All Method –Construction of Gomory’s–Fractional Cut Method Constraints–All Integer LPP– Fractional Cut method –Mixed Integer LPP –Branch and Bound method.

UNIT II: Dynamic Programming (13 Hours)

Introduction – The Recursive equation approach – Characteristics of Dynamic programming –Dynamic programming Algorithm –Solution of Discrete D.P.P –Some applications – Solution of LPP by Dynamic programming.

UNIT III: Non-Linear Programming (12 Hours)

Introduction – Graphical Solution – Kuhn-Tucker conditions with non-negative constraints –Quadratic Programming –Wolfe’s Modified–Beale’s Simplex– Method Separable Convex Programming –Separable Programming Algorithm.

UNIT IV: Queueing Theory (15 Hours)

Introduction – Queueing system – Elements of a Queueing system – Operating characteristics of a Queueing system –Deterministic Queueing system –Probability Distributions in Queueing systems –Classifications of Queueing models –Definition of Transient and steady states – Poisson Queueing system.

UNIT V: Simulation (16 Hours)

Introduction –Why Simulation? –Process of Simulation –Simulation models –Event –Type Simulation –Generation of random numbers –Monte–Carlo Simulation –Simulation of Inventory problems –Simulation of a queueing systems –Simulation of maintenance problems – Simulation in Investment and budgeting.

Unit –VI: (02 Hours)

Latest development related to the course during the semester concerned. [For purpose of Continuous Internal Assessment only]

Text Book:

[1] “Operations Research”, by Kanti Swarup, P. Educational Publishers, New Delhi, 7th Edition –2014.

Unit: I Chapter 7 sec 7.1 to 7.7

Unit: II Chapter 13 sec 13.1 to 13.7

Unit: III Chapter 28 sec 28.1 to 28.8

Unit: IV Chapter 21 sec 21.1 to 21.9

Unit: V Chapter 22 sec 22.1 to 22.11

Reference Book:

[1] “Operations Research” by Hamdy A. Taha, Pre Sixth Edition –1998.

Outcomes:

The learners would have the ability to

- Understand the different methods of I.P.P method and mixed integer LPP.
- Acquire knowledge about Dynamic programming.
- Study about Kuhn Tucker conditions and Quadratic programming.
- Understand the concepts of Queueing system –Poisson Queueing system.
- Discuss simulation method and select the suitable technique and the problem.

SEM –I

Hours/Week:6

Credit : 3

Total Hours: 72

Objectives:

**M.Sc. MATHEMATICS
CALCULUS OF VARIATIONS AND
INTEGRAL EQUATIONS
Code: P1R1MTEC1**

ELECTIVE COURSE:1

Int. Marks: 25

Ext. Marks: 75

Max. Marks: 100

- To find the external functions that make the functional attain a maximum or minimum value
- To understand boundary value problems involving certain types of differential equation like Lagrange's equations.
- To study Green's function and its uses.
- To study the influence function.
- To use iterative method for solving equations of the second kind.

Unit I: Calculus of Variations

(15 Hours)

Maxima and Minima - The Simplest Case - Illustrative Examples –Natural boundary conditions and Transition conditions –The Variational notation –The more general case.

Unit II: Applications of Calculus of Variations

(14 Hours)

Constraints and Lagrange multipliers –Variable end points –Sturm-Liouville problems –Hamilton's–Lagrange's principle equations.

Unit III: Integral Equations

(14 Hours)

Introduction –Relations between Differential and Integral Equations –The Green's function –Alternative definition of the Green's function

Unit IV: Linear Equation in Cause and Effect

(13 Hours)

The influence function –Fredholm equations with separable kernels – Illustrative examples.

Unit V: Applications of Integral Equations

(14 Hours)

Hilbert –Schmidt theory –Iterative methods for solving equations of the second kind – The Fredholm theory –Neumann series.

Unit –VI:

(02 Hours)

Latest development related to the course during the semester concerned. [For purpose of Continuous Internal Assessment only]

Text Book:

[1] "Methods applied of Mathematics" A–Francis B. Hilderbrand, second edition –Prentice - Hall of India Pvt, New Delhi, 1968.

Unit –I: Chapter 2, Sec: 2.1 –2.6

Unit –II: Chapter 2, Sec: 2.7 –2.11

Unit –III: Chapter 3, Sec: 3.1 –3.4

Unit –IV: Chapter 3, Sec: 3.5 –3.7

Unit –V: Chapter 3, Sec: 3.8 –3.10

Reference Book:

[1] "Linear Integral Equations, –R.P. Theory. Kanwal, Academic Press, New York, 1971.

Outcomes :

The learners would have the ability to

- Acquire the knowledge of natural boundary conditions and transition condition.
- Understand and apply the application of calculus of variations, using Hamilton's principle.
- Know about the applications of Green's function in the integral equation to solve
- Study Fredholm equations with separable kernels.
- Apply iterative methods for solving equations of the second kind, using Fredholm theory.

SEM –I
Hours/Week: 6
Credit : 3
Total Hours: 72
Objectives:

M.Sc. MATHEMATICS
ADVANCED NUMBER THEORY
Code: P1R1MTEC1

ELECTIVE COURSE:1
Int. Marks: 25
Ext. Marks: 75
Max. Marks: 100

- To prove results involving divisibility and greatest common divisors.
- To apply Euler –Fermat’s Theorem to prove . relation
- To apply primitive roots for primes –composite numbers.
- To study perfect and Amicable numbers.
- To find the use a Fibonacci. sequence in p

UNIT I: Number Theoretic Functions

(14 Hours)

The sum and number of divisors-The Mobius Inversion formula –The Greatest Integer Function –An Application to the calendar.

UNIT II: Generalization of Euler’s Theorem

(14 Hours)

Leonhard Euler –Euler’s ϕ -Function –Euler’s ϕ -Function –Some Theorems properties of the ϕ -Function.

UNIT III: Primitive Roots and Indices

(14 Hours)

The order of an Integer Modulo n –Primitive Roots for primes –composite Numbers having primitive Roots –The Theory of Indices.

UNIT IV: Number of Special Form

(13 Hours)

Marin Mersenne –Perfect Numbers –Mersenne Primes and Amicable Numbers –Fermat Numbers.

UNIT V: Fibonacci Number and Continued Fraction

(15 Hours)

Fibonacci –The Fibonacci Sequence –Certain Identities –Involving Fibonacci Numbers - Srinivasa Ramanujan –Finite Continued Fractions –Infinite continued Fractions –Farey Fractions –Pell’s Equation.

Unit –VI:

(02 Hours)

Latest development related to the course during the semester concerned. [For purpose of Continuous Internal Assessment only]

Text Book:

[1] “Elementary Number Theory”–Hill Edition by. David 2012. M. Burt

UNIT I: Chapter 6

UNIT II: Chapter 7

UNIT III: Chapter 8

UNIT IV: Chapter 11

UNIT V: Chapter 14 and 15

Reference Books:

[1] “Basic Number Theory” by S.B. Malik, Second [2] Number “ Theory” by Hari-2017 Krishnan,. Twelfth Edition

Outcomes:

The learners would have the ability to

- To study the Mobius Inversion formula.
- Acquire the knowledge of ϕ -function.
- Learn about primitive roots and indices.
- Acquire the knowledge of number of special form.
- Demonstrate an in –depth understanding of Fibonacci sequences and Srinivasa Ramanujan finite continued fractions.

SEM –I	M.Sc. MATHEMATICS	ELECTIVE COURSE:1
Hrs/Week: 6	FUZZY MATHEMATICS AND ITS APPLICATION	Int.Marks: 25
Credit : 3	Code: P1R1MTEC1	Ext.Marks: 75
Total Hrs: 72		Max.Marks:100

Objectives:

- To provide the knowledge of operations on fuzzy sets.
- To introduce the mathematical field on the concept of a fuzzy numbers.
- To enable the students to develop fuzzy relations.
- To use direct methods with one expert and multiple experts.
- To know the applications of fuzzy methodology.

UNIT I: Operations on Fuzzy Sets (14 Hours)

Fuzzy Intersections: t-norms –Fuzzy Unions: t-conorms –Combinations of Operations – Aggregate Operations.

UNIT II: Fuzzy Arithmetic (14 Hours)

Fuzzy Numbers –Linguistic Variables –Arithmetic Operations on Intervals –Arithmetic Operations on Fuzzy Numbers –Lattice of Fuzzy Numbers –Fuzzy Equations.

UNIT III: Fuzzy Relations (14 Hours)

Fuzzy Equivalence Relations –Fuzzy Compatibility Relations –Fuzzy Ordering Relations – Fuzzy Morphisms – sup-i Compositions of Fuzzy Relations – Inf- ω_I Compositions of Fuzzy Relations.

UNIT IV: Constructing Fuzzy Sets and Operations on Fuzzy Sets (15 Hours)

General Discussion –Methods of Construction: An Overview –Direct Methods with One Expert –Direct Methods with Multiple Experts –Indirect Methods with one Expert –Indirect Methods with Multiple Experts - Constructions from Sample Data.

UNIT V: Applications (13 Hours)

Introduction –Medicine –Economics –Fuzzy Systems and Genetic Algorithms –Fuzzy Regression –Interpersonal Communication –Other Applications.

Unit –VI: (02 Hours)

Latest development related to the course during the semester concerned. [For purpose of Continuous Internal Assessment only]

Text Book:

[1] “Fuzzy sets and Fuzzy logic”, George J.Klir
1995.

UNIT I : Chapter 3 (Section 3.3 –3.6)

UNIT II : Chapter 4 Fully

UNIT III : Chapter 5 (Section 5.5 –5.10)

UNIT IV : Chapter 10 Fully

UNIT V : Chapter 17 Fully

Reference Books:

[1] „Fuzzy set theory and–H.J.Zimmermanitsapplications“,2013. Se [2],„Fuzzy Logic with Engineering HillApplications“International Editions-1997.

Outcomes:

The learners would have the ability to

- Discuss the types of operations on fuzzy sets, t- norms and fuzzy arithmetic.
- Study knowledge of fuzzy equivalence relations.
- Identify fuzzy relations, binary fuzzy relations and fuzzy equivalence relations.
- Gain the knowledge of constructing fuzzy sets and operations on fuzzy sets.
- Apply the fuzzy models to natural science and technical fields.

SEM –II
Hours/Week: 6
Credit : 3
Total Hours: 72
Objectives:

M.Sc. MATHEMATICS
NUMERICAL ANALYSIS
Code:P2R1MTEC2

ELECTIVE COURSE:2
Int. Marks: 25
Ext. Marks: 75
Max. Marks: 100

- To understand the concept of transcendental and polynomial equations.
- To know the eigen values and eigen vectors and matrices.
- To know the techniques of Numerical Differentiation and Numerical Integration.
- To know how to use iterative methods to solve systems of linear equations.
- To develop skills in using shooting method and finite elements methods.

Unit I: Transcendental and Polynomial Equations (14 Hours)

Iteration Methods Based on Second degree equation - Rate of convergence - General Iteration Methods-System of non-linear equations - Methods for Complex Roots-Polynomial equations.

Unit II: Eigen Values and Eigen Vectors (16Hours)

Eigen values and Eigen vectors-Jacobi Method for Symmetric Matrices - Givens Method for Symmetric Matrices –Householder's method- Rutishauser for symmetric Method for Arbitrary Matrices - Power Method - Inverse Power Method.

Unit III: Interpolation and Approximation (14 Hours)

Interpolating Polynomials using Finite Differences - Hermite Interpolations - Piecewise and Spline Interpolation - Bivariate Interpolation-Approximation- Least Square Approximation.

Unit IV: Differentiation and Integration (14 Hours)

Numerical Differentiation - Optimum Choice of Step-Length-Extrapolation methods- Numerical Integration - Methods based on interpolation - Methods based on undetermined coefficients- Composite Integration Methods-Romberg Integration.

Unit V: ODE - Boundary Value Problems:- (12Hours)

Introduction –Initial Value Problem - Shooting Method - Finite Difference Methods –Finite Element Methods.

Unit –VI: (02 Hours)

Latest development related to the course during the semester concerned. [For purpose of Continuous Internal Assessment only]

Text Book:

[1] Numerical Methods “Scientific and Engineering Computation”, sixth edition by M.Ked.Jain, Iyengar and R.K.Jain, New Age International (P) Ltd. Reprint- 2012.

Unit I : Chapter 2 Sec 2.4 to 2.9 (page No. 29-99)

Unit II: Chapter 3 Sec 3.5 to 3.12 except 3.6 (Page No. 170-173 & 179-200)

Unit III : Chapter 4 Sec 4.4 to 4.9 (Page No. 235-301)

Unit IV : Chapter 5 Sec 5.2 to 5.4 and 5.6 to 5.10 (Page No. 320-342)

Unit V: Chapter 7 Sec 7.1 to 7.4 (Page No. 550-630)

Reference Books:

[1] S.S.Sastry, “Introduction to Numerical Methods”, Prentice of Hall of Numerical India, New Delhi, (1998).

[2] R.L.Burden and J.Douglas Fairis, “Numerical Analysis”, P.W.S.Kent Publishing company, Boston (1989), Fourth Edition.

Outcomes:

The learners would have the ability to

- Understand the fundamentals of solutions of Algebraic and transcendental equations.
- Understand how use Householder's method, power method
- Acquire knowledge to use hermite interpolation and least square approximation.
- Be familiar with interpolation and extrapolation method.
- Use shooting method, to solve initial value problem.

SEM –II
Hours/Week: 6
Credit : 3
Total Hours: 72
Objectives:

M.Sc. MATHEMATICS
AUTOMATA THEORY
Code:P2R1MTEC2

ELECTIVE COURSE:2
Int. Marks: 25
Ext. Marks: 75
Max. Marks: 100

- *To construct finite state machines and the equivalent regular expressions.*
- *To provide the equivalence of languages described by finite state machines and regular expressions.*
- *To construct pushdown automata and the equivalent content tree grammars.*
- *To construct model for regular languages*
- *To study finite automata and regular expressions.*

Unit I: Mathematical Background and Languages (14 Hours)

Sets –Relations –Graphs –proofs –Formalization of languages –Expressions and grammars: Expressions –grammars.

Unit II: Automata (12Hours)

Conceptualization of automata –Transducers –computability –Exercise.

Unit III: Regular Languages (16Hours)

Regular Expressions –Finite Automata: Basic Definitions –Elimination of ϵ -moves.

Unit IV: Models for Regular Languages (14Hours)

Determinism –simplification- Minimization.

Unit V: Finite Automata and regular expressions (14Hours)

From regular expressions to finite automata: Conversion of regular expressions to finite automata –Scanning.

Unit –VI: (02Hours)

Latest development related to the course during the semester concerned[For purpose of Continuous Internal Assessment only]

Text Book:

[1] “Automata–TheoryandLanguagesandApplications”, Ale international Edition, 2005.

Unit I : Part I sec 0.1 to 0.4 and Chapter 1 sec 1.1, 1.2: 1.2.1 and 1.2.2 only

Unit II : Chapter 2 sec 2.1 to 2.3

Unit III : Chapter 3 sec 3.1, 3.2: 3.2.1 and 3.2.2 only

Unit IV : Chapter 3 sec 3.2: 3.2.3 to 3.2.5

Unit V : Chapter 3 sec 3.3: 3.3.1 –3.3.1.1 and 3.3.1.2

Reference Book:

[1] “Introduction to Automata Theory,roft, Lang

Rajeev Motwani and Jeffrey D. Uiman, Pearson publications, 3rd Edition.

Outcomes:

The learners would have the ability to

- *Apply Automata concepts and techniques in designing systems that address real world problems.*
- *Understand the connection between language and computation.*
- *Analyze the computational strengths and weakness of these machines.*
- *Demonstrate an in-depth understanding of theories, concepts and techniques in automata and their link to computation.*
- *The conversion opf regular expression to finite automata –scanning.*

SEM –II
Hours/Week: 6
Credit : 3
Total Hours: 72
Objectives:

M.Sc. MATHEMATICS
COMBINATORIAL MATHEMATICS
CODE:P2R1MTEC2

ELECTIVE COURSE:2
Int. Marks: 25
Ext. Marks: 75
Max. Marks: 100

- To learn core ideas in combinatorial mathematics.
- To learn about countable sets combinations.
- To become familiar with fundamental combinatorial structures.
- To be familiar with convolution and counting technique.
- To find n^{th} order relations.

Unit I: Principles of Counting –I (13Hours)

The Rules of sum and product- The sum Rule, The product rule- Permutations- Combinations- Binomial and Multinomial Theorems- Combinations with Repetitions.

Unit II: Principle of Counting - II (15 Hours)

Catalan Numbers, Problem of Catalan Numbers - Ramsey Numbers; Introduction , theorem on Ramsey Number with Examples- Strirling Numbers; Introduction- Strirling Numbers of First kind and second kind- Bell Numbers.

Unit III: Principles of Counting - III (13 Hours)

The Pigeonhole principle; Generalization theorem –Principle of inclusion- Exclusion: Principle of inclusion for n sets; Generalization theorem- Problems.

Unit IV: Generating Functions (15 Hours)

Ordinary generation function; Generating functions, Properties and Problems of ordinary generating function- Convolution of sequences-summation using convolution, problems of convolution of sequences- A counting Technique: Problems of a counting Technique- Partitions of integer.

Unit V: Recurrence Relations (14Hours)

First- order Relations: Problems of first order Relations- Second –order linear Homogeneous Relations - Problems of Second-order Linear Homogenous Relations - Third and higher-order Linear Homogeneous Relations and Problems.

Unit –VI: (02Hours)

Latest development related to the course during the semester concerned. [For purpose of Continuous Internal Assessment only]

Text Books:

[1]“Graph Theory and Combinatorics”–Bangalore prismby Dr.D. books, 2005.

Unit I: Chapter 5 –sec 5.1,5.2,5.3(5.3.1,5.3.2)

Unit II: Chapter 5–sec 5.4-5.6

Unit III: Chapter 6 –sec 6.1,6.2

Unit IV: Chapter 7 –sec 7.1(7.1.1,7.1.2,7.1.3)

Unit V: Chapter 8 –sec 8.1-8.3

Reference Books:

[1] “Graph–HarrayTheory.F–Addison -”Wesley - 1969.

[2]“Graph Theory with Applications–NarasingaDeo –toPrienticeEngineeriHall of India Pvt. Ltd. –New Delhi - 2000.

Outcomes :

The learners would have the ability to

- Understand the ideas of Combinatorics.
- Study Ramsey numbers and strilling numbers.
- Study about pigeonhole principle.
- Auquire the knowledge generating function and counting technique.
- Use recurrence relations to solve problems of first, second and higher order linear homogeneous relations.

SEM –III	M.Sc. MATHEMATICS	ELECTIVE COURSE:3
Hours/Week: 6	APPLIED MATHEMATICAL STATISTICS	Int. Marks: 25
Credit : 3	Code:P3R1MTEC3	Ext. Marks: 75
Total Hours: 72		Max. Marks: 100

Objectives:

- To Compute and interpret a correlation coefficient and linear regression analysis
- To understand the relationship between point estimate and interval estimation
- To understand the purpose of analysis of variance
- To compute analysis data generated by functional experiments by using analysis of variance.
- To study statistical analysis with 2^n Factorial experiment.

Unit I: Correlation and Regression (14 Hours)

Multiple and partial correlation –Yule's –Notation Plane of Regression –Generalization
–Properties of residuals –Coefficient of multiple correlation –Properties of multiple correlation-coefficient of partial correlation.

Unit II: Theory of Estimation (14 Hours)

Method of estimation –Method of maximum likelihood Estimation - Method of minimum variance –Method of moments –Confidence intervals and confidence limits – confidence intervals of large sample.

Unit III: Non-Parametric Methods (16 Hours)

Introductions - Advantages and Drawbacks of Non-parametric methods over parametric methods –Basic distribution –Wald - Wolfowitz Run test –test for randomness –median test –sign test –Mann-Whitney –Wilcoxon U Test.(Related simple problems)

Unit IV: Analysis of Variance (12Hours)

Introduction –One way classification –Statistical Analysis of the model –Two Way classification –Statistical Analysis of the Model –Analysis of Two-Way classified data with K-Observation per cell.(Related simple problems)

Unit V: Factorial Experiments (14 Hours)

Factorial experiments – 2^2 -Design –Statistical Analysis of 2^2 design –Yate's of Method Computing factorial effect totals - 2^3 Factorial Experiment –Statistical Analysis - 2^2 Factorial experiment.(Related simple problems).

Unit –VI: (02Hours)

Latest development related to the course during the semester concerned. [For purpose of Continuous Internal Assessment only]

Text Books:

[1] “ Fundamentals of Mathematical Statistics”

New Delhi (2002).

[2]”Fundamentals of Applied Statistics”Newby S.C.

Delhi (2007).

Unit I : Chapter : 12sec:12.4 to 12.11 [1]

Unit II : Chapter: 17 sec: 17.6 to 17.7.1 [1]

Unit III: Chapter:18 sec: 18.7 to 18.7.7 [1]

Unit IV: Chapter: 5 sec: 5.1 to 5.4[2]

Unit V: Chapter: 6 sec: 6.8 –6.8.4 [2]

Reference Books:

[1] “Statistics for Management and A.Santha, Scitech “K Publications. Subramani Pvt.Ltd., 2nd Edition.

[2] “Mathematical J.N.Kapur, H .Statistics” C.Saxena, Chand and Co.Publication Ltd.

Outcomes:

The learners would have the ability to

- Acquire the knowledge of multiple and partial correlation.
- Acquire knowledge on Theory of Estimation and methods of estimating a parameter through sampling and test their Goodness.
- Study the advantages and drawbacks of Non – parametric method and test for randomness.
- Know about analysis of one way and two way classifications.
- Understand the concept of Factorial experiment – 2^2 , 2^3 , 2^n .

SEM –III
Hours/Week: 6
Credit : 3
Total Hours: 72
Objectives:

M.Sc. MATHEMATICS
ADVANCED GRAPH THEORY
CODE:P3R1MTEC3

ELECTIVE COURSE:3
Int. Marks: 25
Ext. Marks: 75
Max. Marks: 100

- *To understand some applications of Graph Theory to Practical Problems and Branches of Mathematics.*
- *To practice creative problem solving and improve skills in this area.*
- *To see the simplicity of Graph Theory and combinatorics at make them ubiquitous.*
- *To make Graph Theory easier and to be creative in Research fields .*
- *To study domination in graphs.*

Unit I :Matchings (14 Hours)

Matchings –Definitions –examples - Matchings and Coverings in Bipartite Graphs –Perfect Matchings.

Unit II : Edge Colourings, Independent Sets and Cliques (14 Hours)

Edge Chromatic Number –Vizing’s –Independent Theorem sets –Ramsey’s Theorem.

Unit III : Vertex Colourings (13Hours)

Chromatic Number – Brook’s –Theorem Hajo’s Conjecture–Chromatic Polynomials.

Unit IV : Planar Graphs (15 Hours)

Plane and Planar Graphs – Dual Graphs – Euler’s –Formulae Bridges– Kuratowski’s–The Five Theorem–Colour Theorem –The Four - Colour conjecture.

Unit V : Domination in Graphs (14 Hours)

Dominating sets in Graphs –Sets of Representatives - Applications of Domination Numbers.

Unit –VI: (02 Hours)

Latest development related to the course during the semester concerned. [For purpose of Continuous Internal Assessment only]

Text Book:

[1] “Graph Theory–J.Awith.Bondy–U.SApplications”.RMurty–TheMacmillanPress Ltd.

[2]Fundamentals“ of Domination in Graphs”,T.W.Haynes, S.Hedetniemi and P. J. Slater, 1998, CRC Press.

Unit –I: Chapter 5, Sec: 5.1 –5.3 [1]

Unit –II: Chapter 6, Sec: 6.1 –6.2 and Chapter 7, Sec: 7.1 –7.2[1]

Unit –III: Chapter 8, Sec: 8.1 –8.4[1]

Unit –IV: Chapter 9, Sec: 9.1 –9.6 [1]

Unit –V: Chapter 1, Sec: 1.1 –1.13 [2]

Reference Books:

[1] “Graph –Theory”Harray.F–Addison - Wesley - 1969.

[2] “Graph Theory withEngineeringApplicationsand–NarasinghComputer”Deoto–Eng Prientice Hall of India Pvt. Ltd. –New Delhi - 2000.

Outcomes :The learners would have the ability to

- *Understand matching and coverings*
- *Acquire the knowledge of edge coloring an*
- *Know about chromatic number and chromatic polynomials*
- *Characterize planar graphs and solve problems related to trees.*
- *Have a deep knowledge of Doinating and its applications.*

SEM –III
Hours/Week: 6
Credit : 3
Total Hours: 72

M.Sc. MATHEMATICS
INTEGRALS OF SPECIAL FUNCTIONS
Code:P3R1MTEC3

ELECTIVE COURSE:3
Int. Marks: 25
Ext. Marks: 75
Max. Marks: 100

Objectives:

- To study about classical polynomials, special functions and their properties
- To learn the Orthogonal Properties of $T_n(x)$ and $U_n(x)$.
- To study Rodrigues formula
- To study Elliptic function
- To study Orthogonal sets of function

Unit I: Hermite polynomials

(14 Hours)

Introduction - Solution of Hermite's equation - Hermite differential polynomials - Generating functions - value of $H_n(x)$ and its derivative at $x=0$ - Rodrigues formula for $H_n(x)$ - Other form of Hermite polynomials - First few Hermite Polynomials - Recurrence Relations for $H_n(x)$ - Hermite's differential equation.

Unit II: Laguerre polynomials and Chebyshev Polynomials

(15 Hours)

Introduction - solution of Laguerre's - Generating Differential Function - Rodrigue's - Recurrence Formula Relations - Laguerre Polynomials for Particular Value of n and x - Differential Equation of $L_n(x)$ - Orthogonal Property of $L_n(x)$ - Other Integral Relation - Independent solution of Chebyshev's - Expansion of $T_n(x)$ Equation and $U(x)$ - Generating Functions - Recurrence Relations - To determine $T_n(x)$ and $U_n(x)$ for given value of n - Orthogonal Properties of $T_n(x)$ and $U_n(x)$.

Unit III: Jacobi Polynomials

(14 Hours)

Introduction - Generating Function - Rodrigues Formula - Orthogonal Properties - Some implications of orthogonality - Recurrence Relations - Relations in which Shift of n is involved - Relations in which n are involved - Shifts - Expansions in $\sin$ - More α , Generating β and Relations - Some properties of Tchebycheff Polynomials.

Unit IV: Elliptic Functions

(13 Hours)

Introduction - Weierstrass' Elliptic $P(z)$ - Differential Equation Function Satisfied by $P(z)$ - Jacobian Theta Function - Zeros of Theta Functions - Some Important Relations - Differential Equation Satisfied by Theta Functions - Jacobian Elliptic Function $S_n(u)$ - Jacobian Elliptic Functions $c_n(u)$ and $d_n(u)$.

Unit V: Orthogonal sets of Functions

(14 Hours)

Introduction - Definitions - Orthogonal set of Functions - Gram-Schmidt Process of Orthogonalization - Orthogonality with respect to Weight Function - Orthogonal set of functions with respect to weight function - Orthonormal set of functions with respect to weight function - Complete Set - Generalised Fourier Series and Fourier constants (Application of Orthogonality) - Sturm-Liouville Problem - Eigen (or Characteristic) Functions - Properties of Eigen Functions and Eigen Values.

Unit –VI:

(02 Hours)

Latest development related to the course during the semester concerned. [For purpose of Continuous Internal Assessment only]

Text book:

[1] "Special Functions"- Saran, Sharma, Trivedi -Pragati Prakashan Educational Publishers.

Unit I: Chapter 7 -sec 7.1,7.2

Unit II: Chapter 8 -sec 8.1-8.9 & Chapter 9 -sec 9.1-9.7

Unit III: Chapter 10 -sec 10.1-10.8

Unit IV: Chapter 11 -sec 11.1-11.9

Unit V: Chapter 12 -sec 12.1-12.10

Reference books:

[1] "Special Functions-R.and Simmon, their Dover books. Applications"

Outcomes: The learners would have the ability to

- Be familiar with Hermite polynomials and Hermite differential equations
- Study about Laguerre polynomials and Chebyshev polynomials
- Acquire knowledge of Rodrigues formula - Recurrence relations and Properties of Tchebycheff polynomials
- Have a deep knowledge of Elliptic Functions and Jacobian elliptic functions
- Know about orthogonality with respect to Weight function and Sturm-Liouville's problem

SEM –IV
Hours/Week: 6
Credit : 3
Total Hours: 72
Objectives:

M.Sc. MATHEMATICS
ADVANCED MATLAB
Code:P4R1MTEC4

ELECTIVE COURSE:4
Int. Marks: 40
Ext. Marks: 60
Max. Marks: 100

- To apply Computer theory and algorithmic aspects in various situations.
- To design and debug the programs.
- To develop program skills independently themselves.

LIST OF PRACTICALS

1. MATLAB program involving matrix manipulation.
Sec: 3.7 - 3.10.3 [1], Page: 48 –68
2. MATLAB program to find Eigen Values and Eigen Vectors
Sec: 8.1 [2], Page: 371 –373
3. MATLAB program to solve a system of linear equations using matrix method.
Sec: 2.3 [2], Page: 92
4. MATLAB program to solve polynomial equation.
Sec: 4.1 –4.11 [1], Page: 81 –89.
5. MATLAB program to draw two-dimensional plots.
Sec: 6.1 and 6.2[1], Page: 120 –129.
6. MATLAB program to draw multiple plots.
Sec: 6.3[1] Page: 129 –131
7. MATLAB program to draw style options, legend command and sub plots.
Sec: 6.4 –6.6, Page: 132 –135
8. MATLAB program to draw Three Dimensional plots.
Sec: 6.8.1 –6.8.8, Page: 146 –151
9. MATLAB program to solve constrained optimization.
Sec: 7.3.2[2], Page: 352 –355
10. MATLAB program to solve Graphical LPP.
Sec: 7.3.3[2], Page: 355 –357
11. MATLAB program to solve Laplace Transform and Inverse Laplace Transform.
Sec: 11.2[1] Page: 265 –266
12. MATLAB program to solve partial Fractions expansion.
Sec: 11.4[1], Page: 267 –269
13. MATLAB program to solve transfer function representation
Sec: 11.5[1], Page: 270 –271
14. MATLAB program to solve Zeros, Poles and Pole –Zero map of a transfer function
Sec: 11.6[1], Page: 272

Unit –VI:

Latest development related to the course during the semester concerned. [For purpose of Continuous Internal Assessment only]

TEXT BOOKS:

- [1] “MATLAB and Its Applications in Engineering”By Raj Kumar Bansal, Ashok Kumar Goel, Manoj Kumar Sharma - Dorling Kindersely (India) Pvt. Ltd.,
[2] “Applied Numerical Methods using MATLAB”By Won Young Yang, Wenwu Cao, Tae –Sang Chung, John Morris, A John Wiley and sons Inc Publications

Outcomes:

The learners would have the ability to

- Express programming and simulation for engineering problems.
- Find importance of this software for lab experimentation.
- Perform and evaluate the relational and logical operations.

SEM –IV
Hours/Week: 6
Credit : 3
Total Hours: 72

M.Sc. MATHEMATICS
GRAPH ALGORITHMS
CODE:P4R1MTEC4

ELECTIVE COURSE:4
Int. Marks: 25
Ext. Marks: 75
Max. Marks: 100

Objectives:

- To identify a connected graph that is a spanning tree.
- To identify whether a graph has a Hamiltonian circuit or path, Eulerian circuit.
- To find a shortest path spanning tree in a graph or digraph.
- To find the components of a graph and the strongly connected components of a digraph.
- To study Hamiltonian algorithm for Maximum matching

UNIT I: An Introduction to Graphs (15 Hours)

Definitions and basic concepts –Distance, Radius, Diameter and Girth –Sub graphs and Isometric sub graphs –Operations on Graphs –The Adjacency, Incidence and Path matrices – Algorithms: Introduction to Algorithms – Breadth-first search Algorithm – Dijkstra’s –Ford’s Algorithm

UNIT II: Graphic Sequences (14 Hours)

Degree sequences – Graphic sequences – Wang and Kleitman’s – Algorithms: Algorithm 1 –Algorithm 2

UNIT III: Eulerian Graphs (12 Hours)

Characterisations of Eulerian Graphs –Degree sets –Randomly Eulerian Graphs – Application –Algorithm –Fleury’s Algorithm

UNIT IV: Hamiltonian Graphs (15 Hours)

Hamiltonian Graphs – Hamilton Cycle in Power Graphs and Line Graphs – Hamiltonian sequences –Application –Algorithms: Two Optimal Algorithm –The Closest Iteration Algorithm –Albertson’s –Related Algorithm parameters

UNIT V: Matchings (14 Hours)

Matching –System of Distinct Representatives and marriage problem –Covering -1- Factor –Stable Matchings –Application –Algorithm: The Hungarian Algorithm –Algorithm for Maximum matching

Unit –VI: (02 Hours)

Latest development related to the course during the semester concerned. [For purpose of Continuous Internal Assessment only]

Text Book:

[1] “Topics in Graph Theory and Algorithms
Publishing House.

Unit I: Chapter 1: Sections 1.1, 1.8 to 1.12

Unit II: Chapter 2: Sections 4.1 to 4.4

Unit III: Chapter 5: Sections 5.1 to 5.5

Unit IV: Chapter 5: Sections 5.7 to 5.12

Unit V: Chapter 6: Sections 6.1 to 6.7

Reference Books:

- 1) “Graph Theory”,-2013,SureshNewDelhi,PHISinghLearningPvt. ., LtdG,.
- 2) “Graph and Combinatorics”,D.S–2005,BangaloreChandrasehaariPrismBooks.

Outcomes:

The students will be able to

- Understand some applications of graph theory to practical problems and other branches of Mathematics.
- Learn about how graph theory and combinatorics developed via a creative organic historical process.
- Use Kruskal’s algorithm to form a spanning tree